

Unit 3 Representation of Data & Instructions



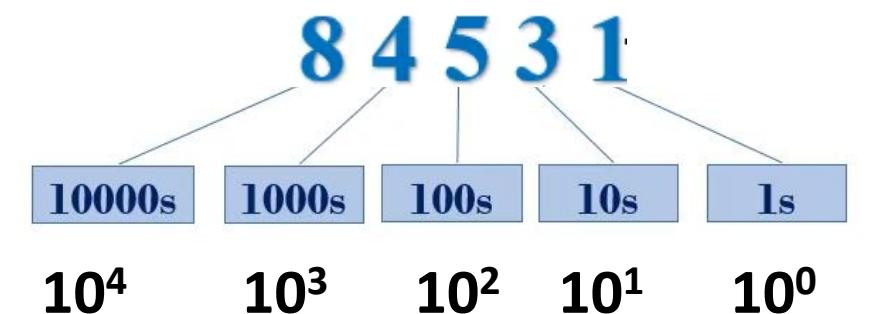
Use of Numbers in Real World

- To represent values
- To calculate
- To count



Use of Numbers in Real World

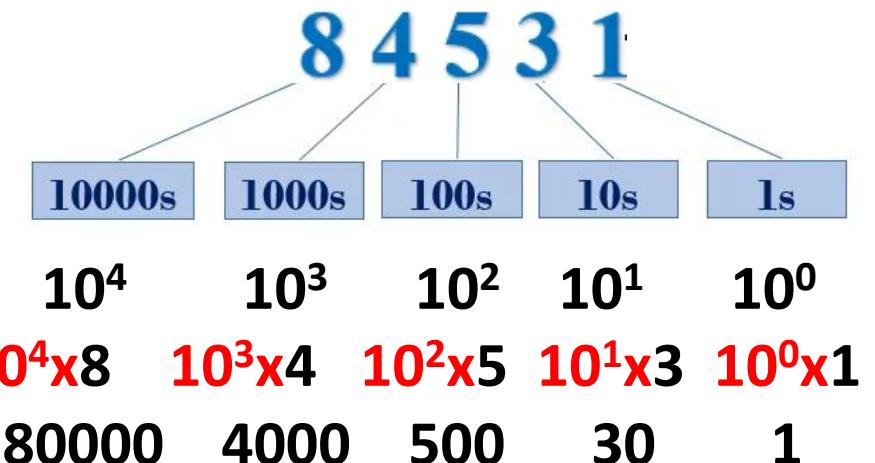
POSITION	4	3	2	1	0
10^{position}	10^4	10^3	10^2	10^1	10^0
Position value	10000	1000	100	10	1
DIGITS	8	4	5	3	1
Digits value	$8 \cdot 10^4$	$4 \cdot 10^3$	$5 \cdot 10^2$	$3 \cdot 10^1$	$1 \cdot 10^0$



$$\begin{aligned}
 & 10^4 \times 8 \quad 10^3 \times 4 \quad 10^2 \times 5 \quad 10^1 \times 3 \quad 10^0 \times 1 \\
 & 80000 \quad 4000 \quad 500 \quad 30 \quad 1
 \end{aligned}$$

**Decimal
Number System**

Use of Numbers in Real World



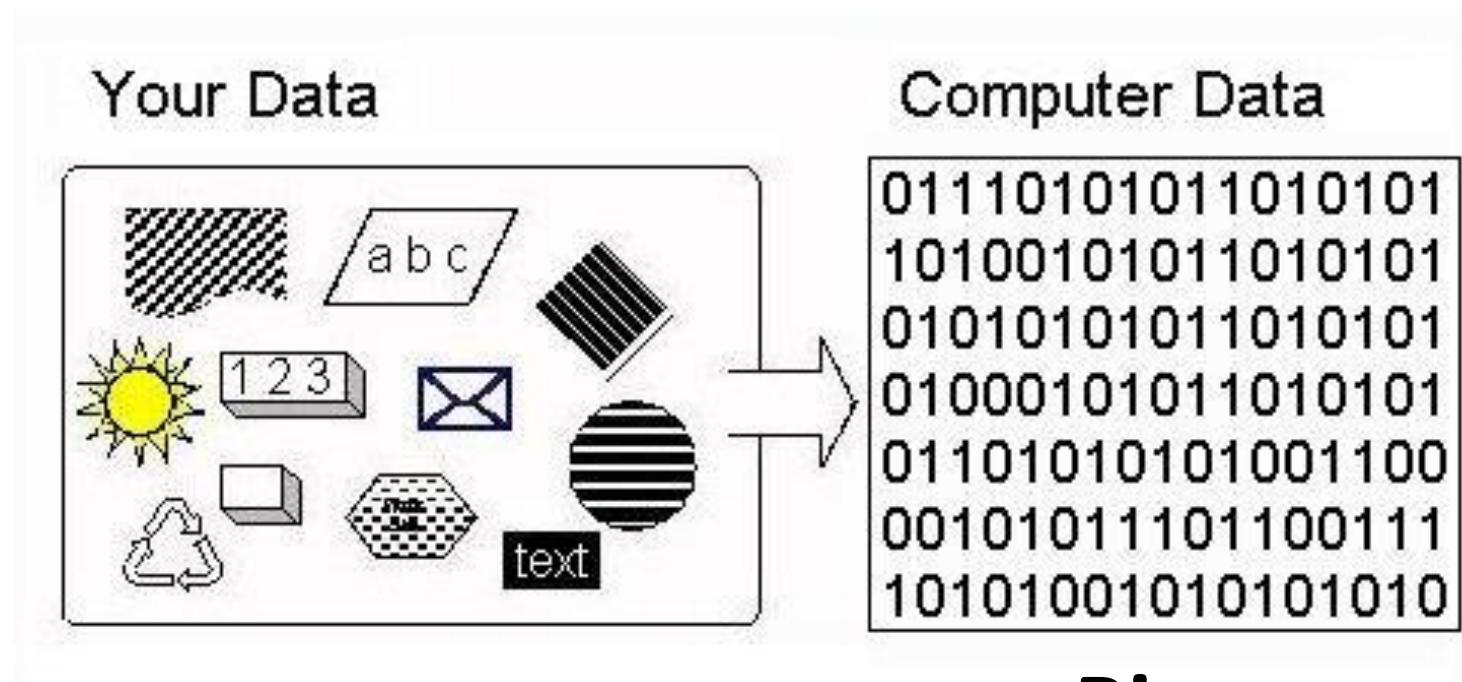
MSD
Most
Significant
Digit

8 4 5 3 1

LSD
Least
Significant
Digit

Decimal
Number System

Data Representation in Computers



**Binary
Number System**

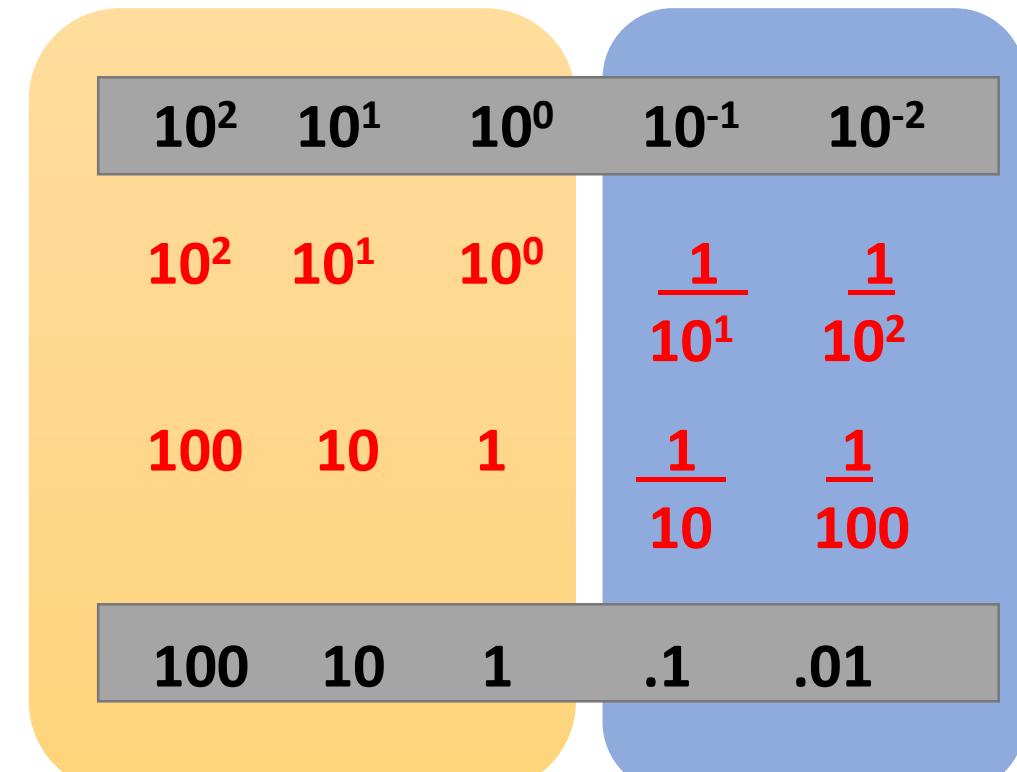
Data Representation in Computers

Number Systems		
System	Base	Digits
Binary	2	0 1
Octal	8	0 1 2 3 4 5 6 7
Decimal	10	0 1 2 3 4 5 6 7 8 9
Hexadecimal	16	01 2 3 4 5 6 7 8 9 A B C D E F

Decimal Number System

Number Systems		
System	Base	Digits
Decimal	10	0 1 2 3 4 5 6 7 8 9

536.23

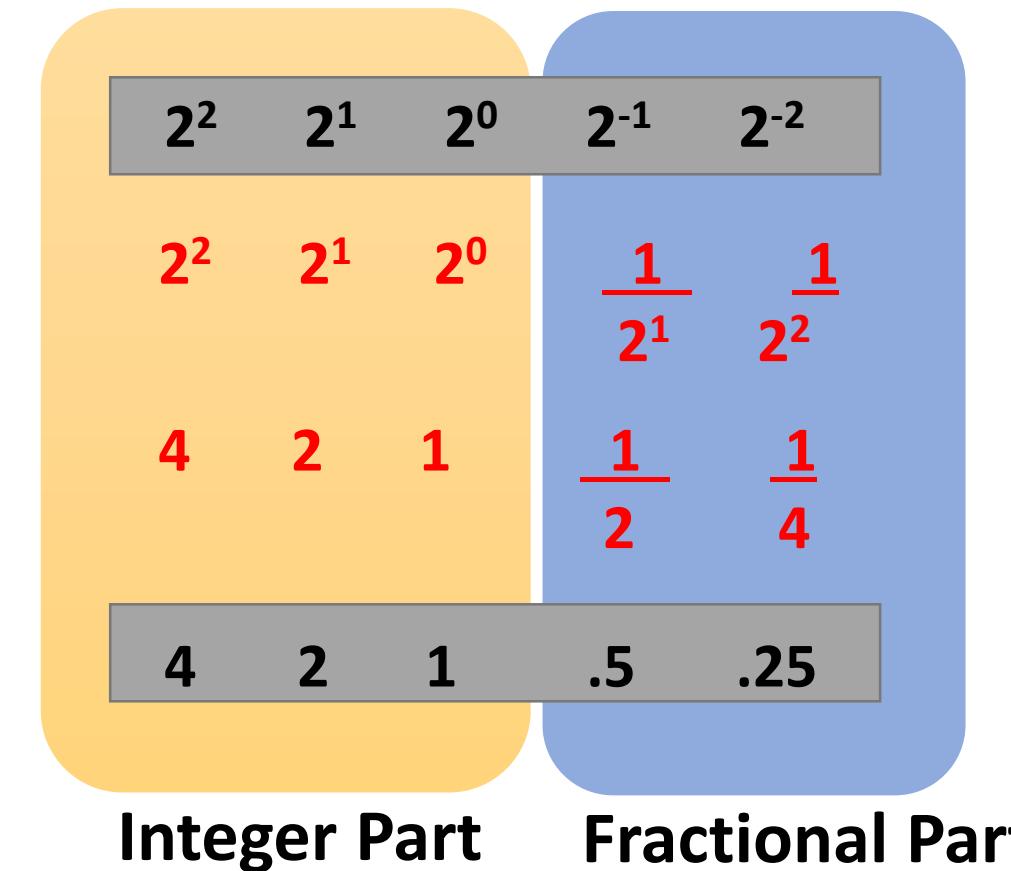


Integer Part

Fractional Part

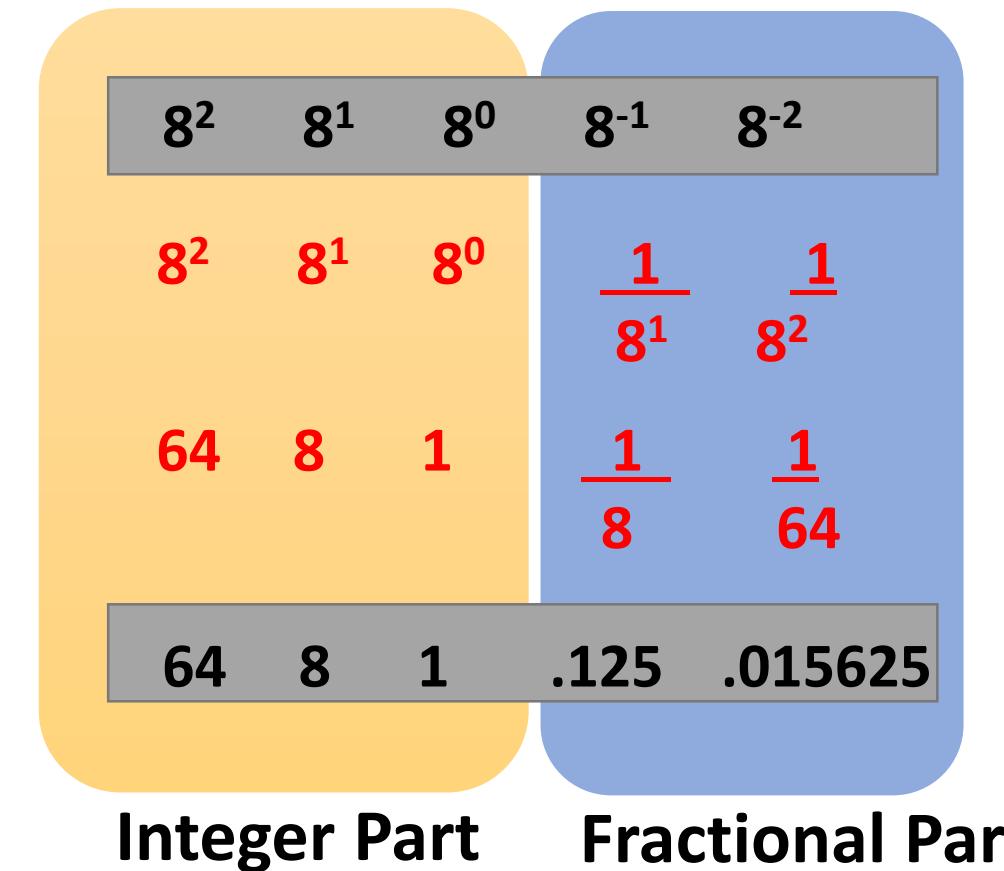
Binary Number System

Number Systems		
System	Base	Digits
Binary	2	0 1



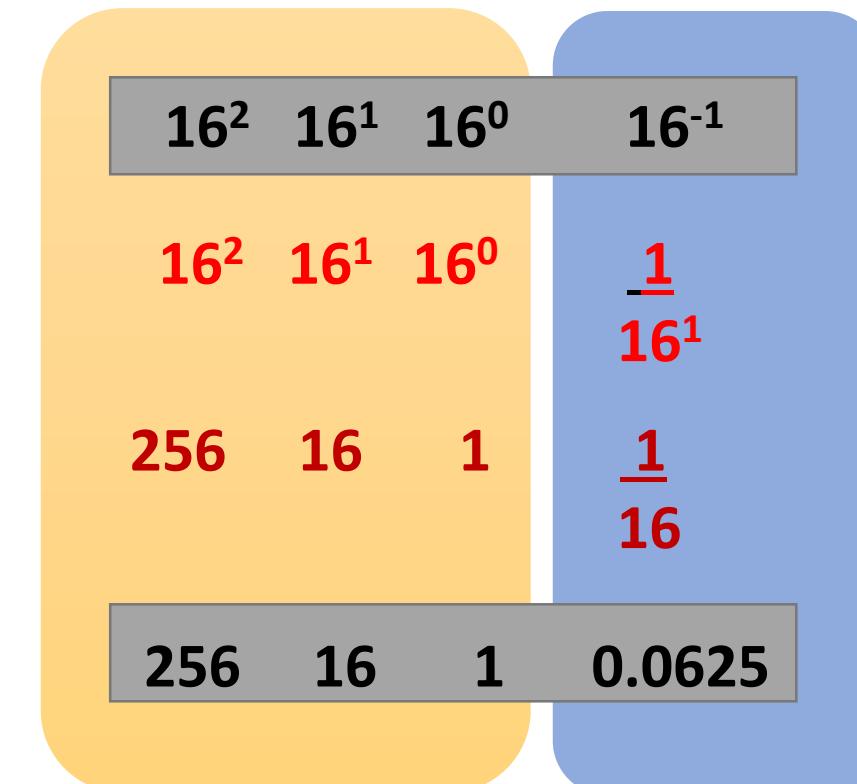
Octal Number System

Number Systems		
System	Base	Digits
Octal	8	0 1 2 3 4 5 6 7

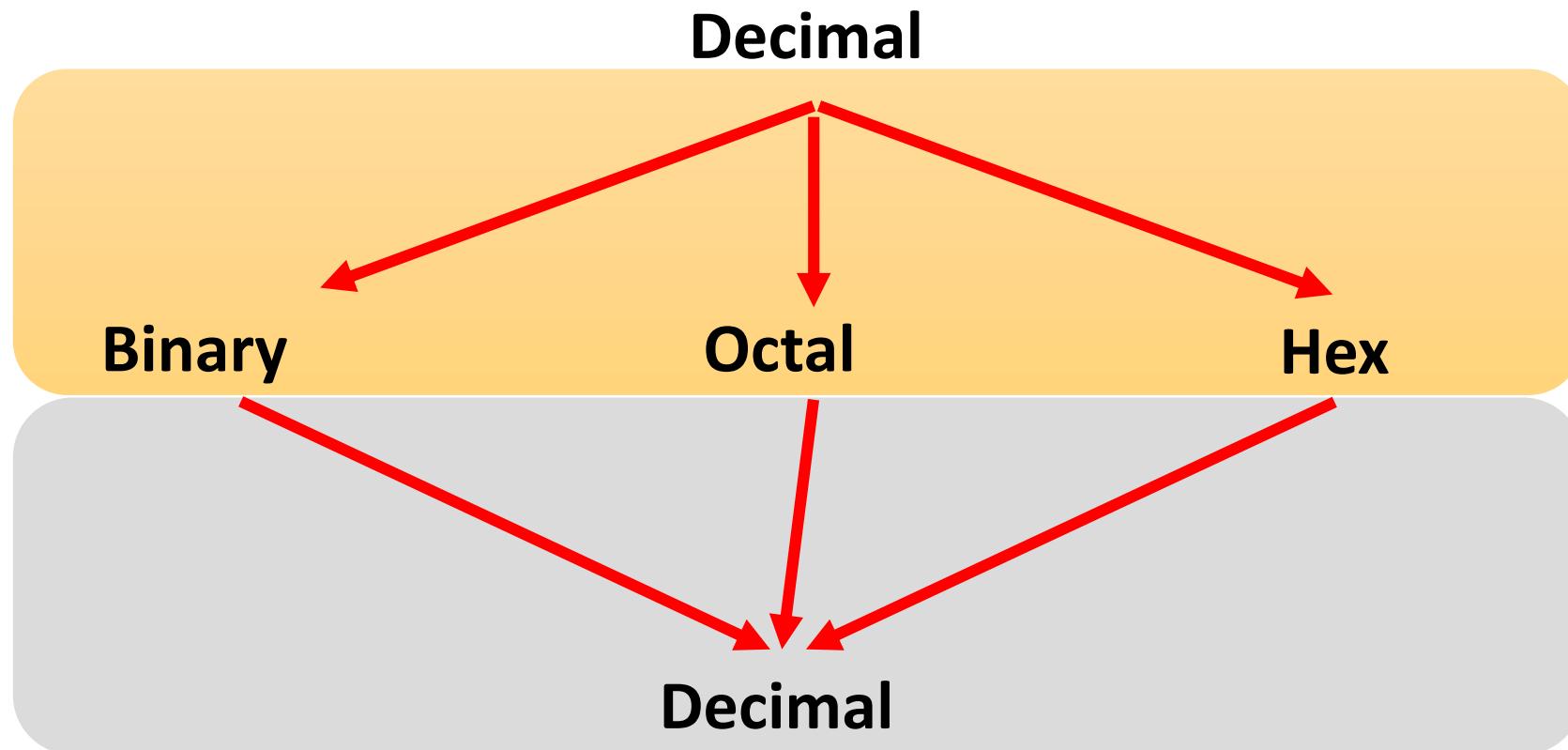


Hexa-Decimal Number System

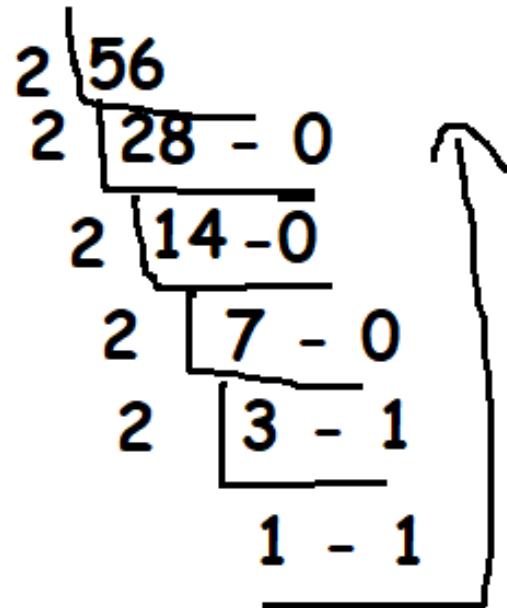
Number Systems		
System	Base	Digits
Hexadecimal	16	0 1 2 3 4 5 6 7 8 9 A B C D E F



Conversions



Conversion – Decimal to Binary

 $56.125_{10} \rightarrow \text{Binary}$ 

.125	$\times 2$
0	250×2
0	500×2
1	000

 111000 $.001$ 111000.001_2

Conversion – Decimal to Binary

28.0625₁₀ --> Binary

$$\begin{array}{r} 28 \\ \hline 2 | 14 - 0 \\ 2 | 7 - 0 \\ 2 | 3 - 1 \\ 2 | 1 - 1 \end{array}$$

0625 ×2	
0	1250 ×2
0	2500 ×2
0	5000 ×2
1	0000

11100

.0001

11100.0001₂

Conversion – Decimal to Octal

 $28.0625_{10} \rightarrow \text{Octal}$

$$\begin{array}{r} 8 \quad [28] \\ \hline 3 \quad -4 \end{array}$$

$$\begin{array}{r} .0625 \times 8 \\ \hline 0 \quad .5000 \times 8 \\ \hline 4 \quad .0000 \end{array}$$

34

.04

 34.04_8

Conversion – Decimal to Hexa-Decimal

$28.0625_{10} \rightarrow \text{Hexa Decimal}$

$$\begin{array}{r} 16 \quad | \quad 28 \\ \quad \quad \quad \downarrow \\ \quad \quad \quad -C \\ \hline .0625 \times 16 \\ \quad \quad \quad \downarrow \\ \quad \quad \quad 1 \quad 0000 \end{array}$$

1C .1

$1C.1_{16}$

Conversions

28.0625₁₀

Decimal

Binary

$$\begin{array}{r}
 28 \\
 2 \overline{)14} \quad 0 \\
 2 \overline{)7} \quad -0 \\
 2 \overline{)3} \quad -1 \\
 2 \overline{)1} \quad -1
 \end{array}$$

$$\begin{array}{r}
 0.0625 \times 2 \\
 \hline
 0 \quad 1250 \times 2 \\
 0 \quad 2500 \times 2 \\
 0 \quad 5000 \times 2 \\
 \hline
 1 \quad 0000
 \end{array}$$

Octal

$$\begin{array}{r}
 8 \overline{)28} \\
 3 \quad -4 \\
 \hline
 .0625 \times 8 \\
 .5000 \times 8 \\
 .0000
 \end{array}$$

$$\begin{array}{r}
 16 \overline{)28} \\
 1 \quad -C \\
 \hline
 .0625 \times 16 \\
 1 \quad 0000
 \end{array}$$

Hex

111000.001₂**34.04₈****1C.1₁₆**

Conversions - Activity

Decimal

48.125

Binary

Octal

Hex

Decimal

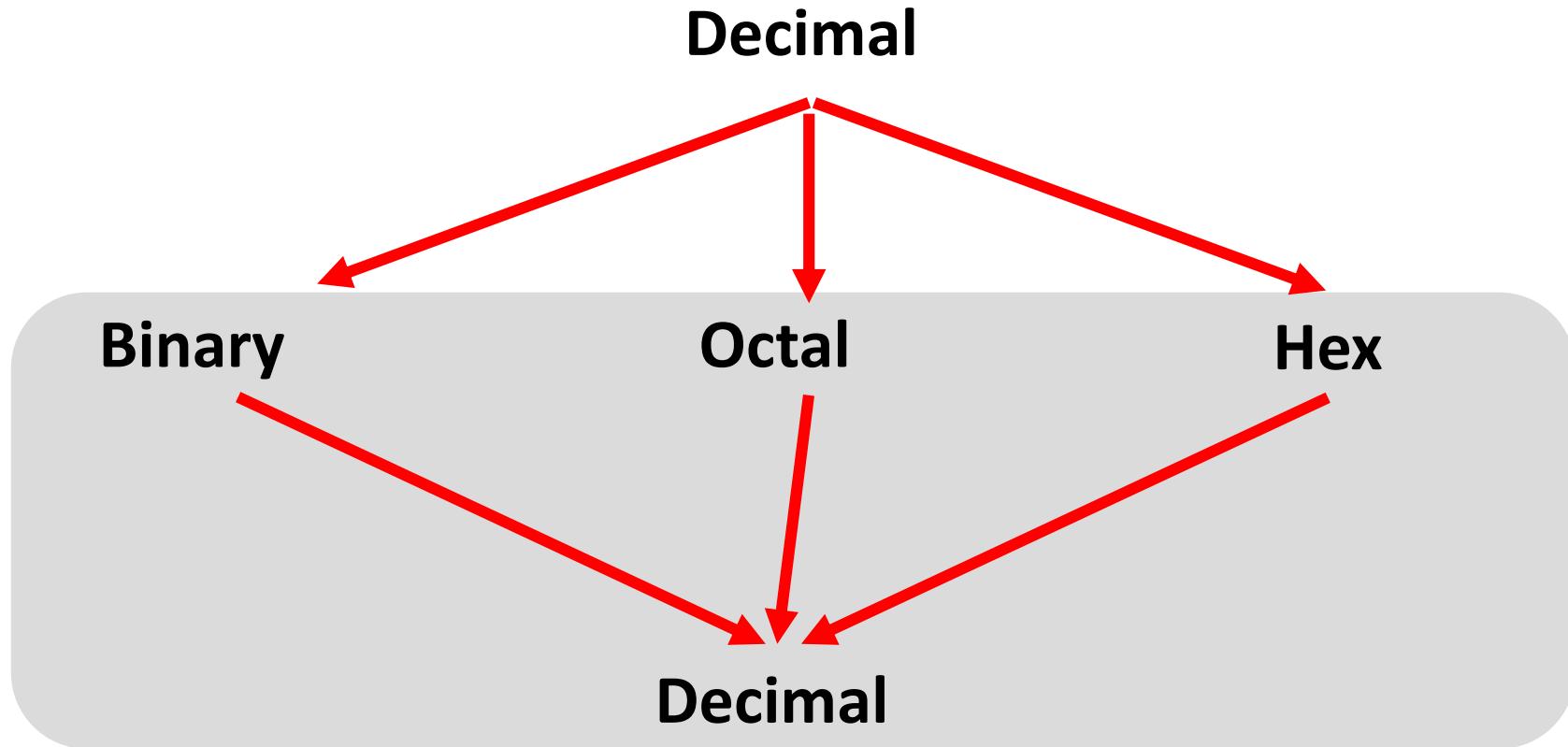
52.12

Binary

Octal

Hex

Conversions



Conversion –Binary to Decimal

111000.001₂ → Decimal

1	1	1	0	0.	0	0	0	1
$2^4 \times 1$	$2^3 \times 1$	$2^2 \times 1$	$2^1 \times 0$	$2^0 \times 0$	$2^{-1} \times 0$	$2^{-2} \times 0$	$2^{-3} \times 0$	$2^{-4} \times 1$
16×1	8×1	4×1	2×0	1×0	.5×0	.25×0	.125×0	.0625×1
16	8	4	0	0.	0	0	0	.0625

28.0625₁₀

Conversion –Octal to Decimal

34.04₈ → Decimal

$$\begin{array}{ccccccc} & 3 & & 4 & . & 0 & 4 \\ 8^1 \times 3 & 8^0 \times 4 & 8^{-1} \times 0 & 8^2 \times 4 & & & \\ 8 \times 3 & 1 \times 4 & 0 \times .125 & 4 \times .015625 & & & \\ 24 & + & 4 & + & 0 & + & 0.0625 \end{array}$$

28.0625₁₀

Conversion – Hexa to Decimal

1C.1₁₆ → Decimal

$$\begin{array}{ccccccc} 1 & & C & . & 1 \\ 16^1 \times 1 & & 16^0 \times C & & 16^{-1} \times 1 \\ 16 \times 1 + & & 12 \times 1 + & & 1 \times .0625 \\ 16 & + & 12 & & .0625 \end{array}$$

28.0625₁₀

Conversions

Binary

$$\begin{array}{ccccccccc}
 1 & 1 & 1 & 0 & 0. & 0 & 0 & 0 & 1 \\
 2^4 & 2^3 & 2^2 & 2^1 & 2^0 & 2^{-1} & 2^{-2} & 2^{-3} & 2^{-4} \\
 2 \times 1 & 8 \times 1 & 4 \times 1 & 2 \times 0 & 1 \times 0 & .5 \times 0 & .25 \times 0 & .125 \times 0 & .0625 \times 1 \\
 16 \times 1 & 8 \times 1 & 4 \times 1 & 2 \times 0 & 1 \times 0 & .5 \times 0 & .25 \times 0 & .125 \times 0 & .0625 \times 1 \\
 16 & 8 & 4 & 0 & 0. & 0 & 0 & 0 & .0625 \\
 & & & & & & & & 28.0625_{10}
 \end{array}$$

Octal

$$\begin{array}{ccccccccc}
 3 & 4 & . & 0 & 4 \\
 8^1 \times 3 & 8^0 \times 4 & 8^{-1} \times 0 & 8^{-2} \times 4 \\
 8 \times 3 & 1 \times 4 & 0 \times .125 & 4 \times .015625 \\
 24 + 4 + 0 + 0.0625 \\
 28.0625_{10}
 \end{array}$$

Hex

$$\begin{array}{ccccccccc}
 1 & C & . & 1 \\
 16^1 \times 1 & 16^0 \times C & 16^{-1} \times 1 \\
 16 \times 1 + 12 \times 1 + 1 \times .0625 \\
 28.0625
 \end{array}$$

28.0625₁₀

Conversions - Activity

Binary

11010.101_2

Octal

275.31_8

Hex

$1A.5_{16}$

Unit 3 Representation of Data & Instructions

